

Solve for x.

$$1. \frac{ax}{x} + \frac{bx}{x} = c$$

$$x \frac{(a+b)}{a+b} = \frac{c}{a+b}$$

$$x = \frac{c}{a+b}$$

$$2. \sqrt{(x-b)^2} = \sqrt{c}$$

$$x-b = \pm \sqrt{c}$$

$$x = \pm \sqrt{c} + b$$
$$x = b \pm \sqrt{c}$$

Deriving the Quadratic Formula

$$ax^2 + bx + c = 0$$
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\left(\frac{ax^2 + bx}{a}\right) + c = 0$$

$$a\left(x^2 + \frac{b}{a}x\right) + c = 0$$

$$\left(\frac{b}{2}\right)^2 = \left(\frac{1}{2} \cdot \frac{b}{a}\right)^2 = \left(\frac{b}{2a}\right)^2 = \frac{b^2}{4a^2}$$

$$a\left(x^2 + \frac{b}{a}x + \frac{b^2}{4a^2}\right) + c = \frac{b^2}{4a}$$

$$a\left(x + \frac{b}{2a}\right)^2 + c = \frac{b^2}{4a}$$

$$\frac{a}{a}\left(x + \frac{b}{2a}\right)^2 - \frac{1}{a}\left(\frac{b^2}{4a}\right) - \frac{c}{a}$$

$$\left(x + \frac{b}{2a}\right)^2 = \frac{b^2}{4a^2} - \frac{c}{a} \frac{4a}{4a}$$

$$\sqrt{\left(x + \frac{b}{2a}\right)^2} = \frac{\sqrt{b^2 - 4ac}}{\sqrt{4a^2}}$$

$$x + \frac{b}{2a} = \frac{\pm \sqrt{b^2 - 4ac}}{2a} - \frac{b}{2a}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$