

Inverse Variation

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Like direct variation, **inverse variation** is defined by a constant of variation. An inverse relationship is modeled by:

$$y = \frac{k}{x} \quad \leftarrow \text{constant}$$

Inverse variation is determined by using:

$$k = yx$$

Ex. 1 y varies inversely as x with a constant of variation of 6. Write an equation.

$$\boxed{y = \frac{6}{x}}$$

Find y if $x = 4$.

$$y = \frac{6}{4}$$

$$\boxed{y = \frac{3}{2}}$$

Find x if $y = 18$.

$$18 = \frac{6}{x}$$

$$18x = 6$$

$$\boxed{x = \frac{1}{3}}$$

Ex. 2 x and y vary inversely. If $x = 3$ when $y = 21$, find the constant and write the equation.

$$K = 21(3) \rightarrow \boxed{y = \frac{63}{x}}$$

$K = 63$

Find x when $y = 7$.

$$7 = \frac{63}{x}$$

$$7x = 63$$

$$\boxed{x = 9}$$

Find y when $x = 10$.

$$y = \frac{63}{10}$$

$$\boxed{y = 6.3}$$

Ex. 3 Determine whether each table shows a direct, inverse, or no variation. If so, find the values.

$\frac{y}{x}$	x	y	yx
6.6	2	13.2	26.4
4.95	4	19.8	79.2
		33	
	8		
6.6	10	66	660

neither

$\frac{y}{x}$	x	y	yx
9.6	3	29	87
3.48	5	17.4	87
	6		
0.87	10	8.7	87
		7.25	

inverse, $k = 87$

$$y = \frac{87}{6} \quad 7.25 = \frac{87}{x}$$

$$\boxed{y = 14.5} \quad \boxed{x = 12}$$

$\frac{y}{x}$	x	y	yx
		10.2	
5.1	3	15.3	45.9
	4		
5.1	6	30.6	183.6
5.1	9	45.9	413.1

direct, $k = 5.1$

$$10.2 = 5.1x \quad y = 5.1(4)$$

$$\boxed{x = 2} \quad \boxed{y = 20.4}$$